



A Proposal of Optimal Strategy for Emptying the Buffer at the MIMO Transmitter based Spatial Multiplexing Techniques

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Abstract: In this paper, we analyse the buffer behaviour in MIMO transmitter, depending on the traffic incoming intensity and service discipline of the outgoing process, respectively, depending on the buffer filling and emptying processes. Using a mathematical study and a simulation model we propose an optimal strategy for employing the buffer at the MIMO transmitter based spatial multiplexing techniques.

Keywords: MIMO, spatial multiplexing, buffers, M/M/1/c.

I. INTRODUCTION

The main characteristic which allows that 802.11n systems has better performances than the previous 802.11a/b/g systems, is MIMO (Multiple-Input Multiple-Output) technology [1]. The main idea of MIMO is to improve quality (BER) and/or data rate (bits/sec) by using multiple antennas at the transmitter and receiver. MIMO technology has attracted attention in wireless communications, because it offers significant increases in data throughput and link range without requiring additional bandwidth or transmit power [2].

There are various categories of MIMO techniques. A commonly used technique is spatial multiplexing [3]. Spatial multiplexing is used to transmit simultaneously independent and separately encoded data signals, so called streams, from each of the multiple transmit antennas, over the same radio frequency channel. Therefore, the space dimension is reused, or multiplexed, more than one time. The main goal of the technique is to achieve high data rates.

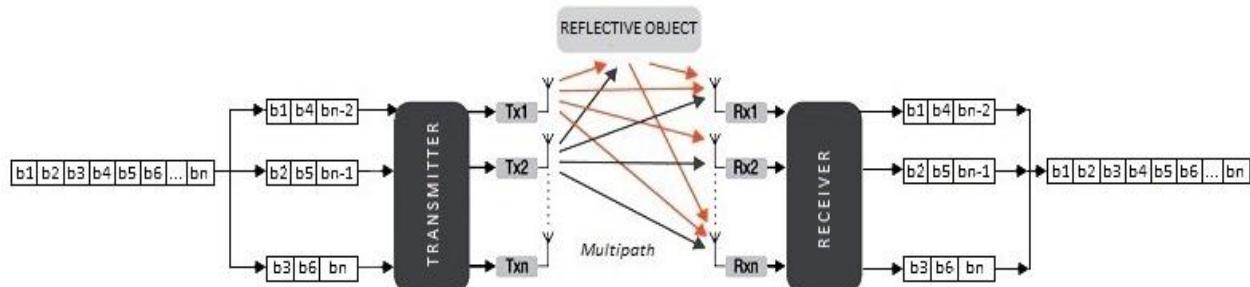


Fig. 1. Spatial multiplexing

We assume that input data packets are buffered at the transmission side of MIMO system, before the packets will be sent to a circuit that performs modulation and mapping of the packets to certain antennas, as shown in Fig. 1.

One of the problems is to determine buffer capacity in a function of traffic intensity, in order to prevent buffer overflow, respectively, packet loss. In this case, it is necessary to determine an optimal strategy for emptying the buffer.

discipline that gives the optimal strategy for emptying the buffer is proposed. Also, results of the analysis and its comparison is described in the Section III. in MIMO systems

II. M/M/1/C MODEL

Data packets ($b_1, b_2, b_3, \dots, b_n$) arrive at the transmission part of MIMO system, and before spatial multiplexing they are stored in buffer with limited capacity C .

The rest of this paper is organized as follows. In Section II, M/M/1/C model is analyzed. In Section III, a model service

We assume that the data packets arrive random from different sources, and the arrival process can be described



as a Poisson process, with parameter λ while the service discipline in the buffer is exponential as well, with parameter μ . Obviously, the system was presented as M/M/1/C model which means in the buffer can be stored C packets[4]. The case when the buffer is empty is included too. If the buffer is full, all packets that arrive will be lost. In this case, appropriate parameters are:

$$\lambda_n = \begin{cases} \lambda & \text{for } n = 0, 1, \dots, c - 1 \\ 0 & \text{for } n = c, c + 1 \end{cases} \quad (1)$$

We will define $\rho = \lambda/\mu$ as the traffic intensity of the system which is a ratio of the arrival and service rates.

For $\rho \in (0, \infty) \setminus \{1\}$, we have:

$$S_0 = (1 + \rho + \rho^2 + \dots + \rho^{c+1})^{-1} = (1 - \rho) / (1 - \rho^{c+2}) \quad (2)$$

and for $\rho = 1$, we have:

$$S_0 = \frac{1}{c+2} \quad (3)$$

where S_0 is the probability that the buffer is empty.

Probability of state of the buffer in a moment when a packet is in a multiplexing queue are:

$$S_n = \rho^n S_0 \quad n = 1, 2, \dots, c \quad (4)$$

Respectively,

$$S_n = \begin{cases} \frac{\rho^n (1-\rho)}{1-\rho^{c+1}} & \text{for } \rho \neq 1 \\ \frac{1}{c+2} & \text{for } \rho = 1 \end{cases} \quad (5)$$

With L we denote the packet error probability, so, effective throughput, T , or probability that the incoming packet will be multiplexed is:

$$T = \lambda (1 - L) \quad (6)$$

The probability of opposite event will be:

$$\bar{T} = 1 - \lambda (1 - L) \quad (7)$$

The packet will not be multiplexed when in the observed interval does not have incoming packets. So, the expression of the expected number of packets that are lost because of overdraft capacity of the buffer will be:

$$L = \rho^{c-1} \frac{1-\rho}{1-\rho^{c+2}} \quad (8)$$

III. RESULTS ANALYSIS

Firstly, let us review the basic foundations of the model which has been presented in details in [5].

Input flow packets which arrive from different sources are random, so, the statistics of incoming packets in a buffer of limited capacity, are treated as Poisson process. Service discipline of a transmitter is such that buffers empty with constant flow.

The probability of arrival of k packets in a certain time interval is:

$$P_A(k) = \frac{\lambda^k e^{-\lambda}}{k!} \quad (9)$$

where λ is expected number of packets in the interval.

Probability of state of the buffer is given by the expresion:

$$S_n = \sum_{k=0}^n S_k P_A(n-k) \text{ for } 1 \leq n \leq C - 1 \quad (10)$$

The packet error probability is:

$$L = 1 + \frac{S_0 e^{-\lambda} - 1}{\lambda} \quad (11)$$

Secondly, we compare the results obtained in [5] with results obtained using the M/M/1/C model.

We note that the M/M/1/C model is indicated by the full lines and the other model is indicated by the dashed lines.

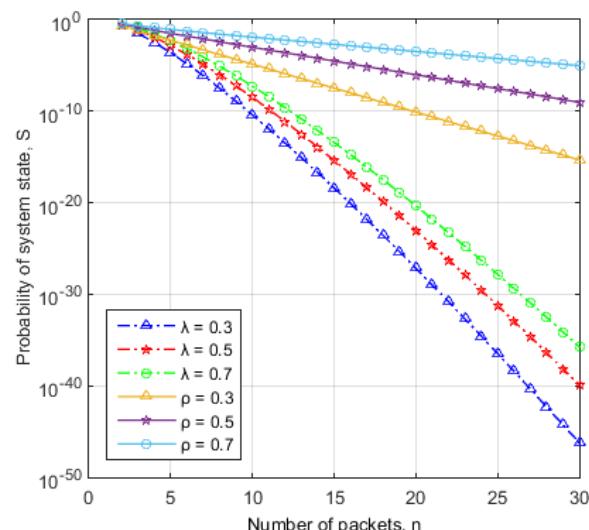


Fig.2. The probability of system state depending on number of Packets

Fig. 2. shows the probability of the system state S depending on numbers of packets n for the chosen values of λ ($\lambda = 0.3$, $\lambda = 0.5$ and $\lambda = 0.7$) and ρ ($\rho = 0.3$, $\rho = 0.5$ and $\rho = 0.7$). It can be seen that the probability of the system state decreases with increasing of the number of packets in the both model but there are differences between them. When the number of packet is very small, the probabilities are almost approximate, but with the increasing the number of packets, the probability of system state of the M/M/1/C model is much higher than the probability of system state of the other model.

Fig. 3. shows the packet error probability depending on the capacity of the buffer due to the buffer capacity distortion for the chosen values of λ ($\lambda = 0.3$, $\lambda = 0.5$ and $\lambda = 0.7$) and ρ ($\rho = 0.3$, $\rho = 0.5$ and $\rho = 0.7$). It can be observed that the packet error probability decrees with increasing of the buffer capacity. With the larger buffer capacity, the packet error probability of the M/M/1/C model is much higher than the packet error probability of the other model.

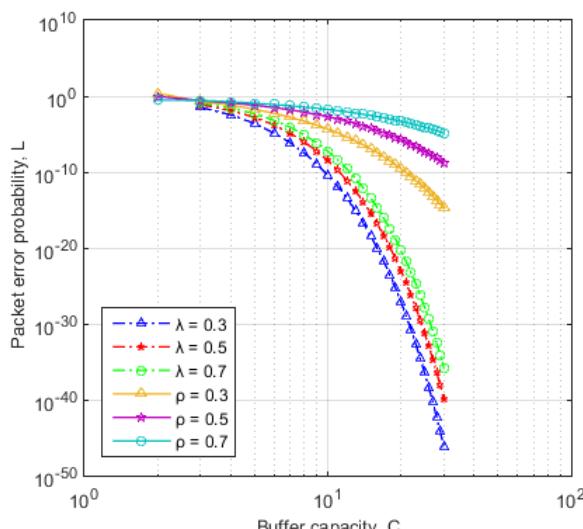


Fig.3. The packet error probability depending on the capacity of the buffer due to the buffer capacity distortion

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IV. CONCLUSION

This paper presents the results obtained by analysing buffer behaviour in MIMO transmitter depending on the buffer filling and emptying processes. Using a simulation model, realized in MATLAB, and the theoretical analysis confirm that the strategy for emptying the buffer with constant output flow is an optimal strategy for emptying the buffer that may well approximate the spatial multiplexing of packets that are buffered and forward them to transmit antennas

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BIOGRAPHY



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